

**ENGINEERING MATHEMATICS-IV**  
**[As per Choice Based Credit System (CBCS) scheme]**  
**(Effective from the academic year 2016 -2017)**  
**SEMESTER – IV**

Subject Code	15MAT41	IA Marks	20
Number of Lecture Hours/Week	04	Exam Marks	80
Total Number of Lecture Hours	50	Exam Hours	03

**CREDITS – 04**

**Course objectives:** This course will enable students to

- Formulate, solve and analyze engineering problems.
- Apply numerical methods to solve ordinary differential equations.
- Apply finite difference method to solve partial differential equations.
- Perform complex analysis.
- Interpret use of sampling theory.
- Apply joint probability distribution and stochastic process

**Module 1** **10 Hours**

**Numerical Methods:** Numerical solution of ordinary differential equations of first order and first degree, Picard's method, Taylor's series method, modified Euler's method, Runge-Kutta method of fourth order. Milne's and Adams-Bashforth predictor and corrector methods (No derivations of formulae). Numerical solution of simultaneous first order ordinary differential equations, Picard's method, Runge-Kutta method of fourth order

**Module 2** **10 Hours**

**Numerical Methods:** Numerical solution of second order ordinary differential equations, Picard's method, Runge-Kutta method and Milne's method. **Special Functions:** Bessel's functions- basic properties, recurrence relations, orthogonality and generating functions. Legendre's functions - Legendre's polynomial, Rodrigue's formula, problems.

**Module 3** **10 Hours**

**Complex Variables:** Function of a complex variable, limits, continuity, differentiability, Analytic functions-Cauchy-Riemann equations in Cartesian and polar forms. Properties and construction of analytic functions. Complex line integrals-Cauchy's theorem and Cauchy's integral formula, Residue, poles, Cauchy's Residue theorem with proof and problems. **Transformations:** Conformal transformations, discussion of transformations:  $z = x + iy$ ,  $w = u + iv$ ,  $z = x + iy = u + iv + (x - u) + i(y - v)$  and bilinear transformations.

**Module 4** **10 Hours**

**Probability Distributions:** Random variables (discrete and continuous), probability functions. Poisson distributions, geometric distribution, uniform distribution, exponential and normal distributions,

Problems. **Joint probability distribution:** Joint Probability distribution for two variables, expectation, covariance, correlation coefficient.

## Module 5

10 Hours

**Sampling Theory:** Sampling, Sampling distributions, standard error, test of hypothesis for means and proportions, confidence limits for means, student's t-distribution, Chi-square distribution as a test of goodness of fit. **Stochastic process:** Stochastic process, probability vector, stochastic matrices, fixed points, regular stochastic matrices, Markov chains, higher transition probability.

### Course Outcomes:

After studying this course, students will be able to:

- Use appropriate numerical methods to solve first and second order ordinary differential equations.
- Use Bessel's and Legendre's function which often arises when a problem possesses axial and spherical symmetry, such as in quantum mechanics, electromagnetic theory, hydrodynamics and heat conduction.
- State and prove Cauchy's theorem and its consequences including Cauchy's integral formula.
- Compute residues and apply the residue theorem to evaluate integrals.
- Analyze, interpret, and evaluate scientific hypotheses and theories using rigorous statistical methods.

### Graduate Attributes

- Engineering Knowledge
- Problem Analysis
- Life-Long Learning
- Conduct Investigations of Complex Problems

### Question paper pattern:

The question paper will have ten questions.

There will be 2 questions from each module.

Each question will have questions covering all the topics under a module.

The students will have to answer 5 full questions, selecting one full question from each module.

### Text Books:

1. B. V. Ramana "Higher Engineering Mathematics" Tata McGraw-Hill, 2006.
2. B. S. Grewal, "Higher Engineering Mathematics", Khanna publishers, 42<sup>nd</sup> edition, 2013.

### Reference Books:

1. N P Bali and Manish Goyal, "A text book of Engineering mathematics", Laxmi publications, latest edition.
2. Kreyszig, "Advanced Engineering Mathematics" - 9th edition, Wiley, 2013.
3. H. K Dass and Er. Rajnish Verma, "Higher Engineering Mathematics", S. Chand, 1<sup>st</sup> ed, 2011.